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**Optimal Placement of Hybrid PV-Wind Systems  
Using Genetic Algorithm**



# Overview

- 1- Introduction
- 2- Hybrid PV-Wind System (HPWS)
- 3- System Structure and Modeling
- 4- System Design and GA Optimization
- Conclusion

# 1- Introduction

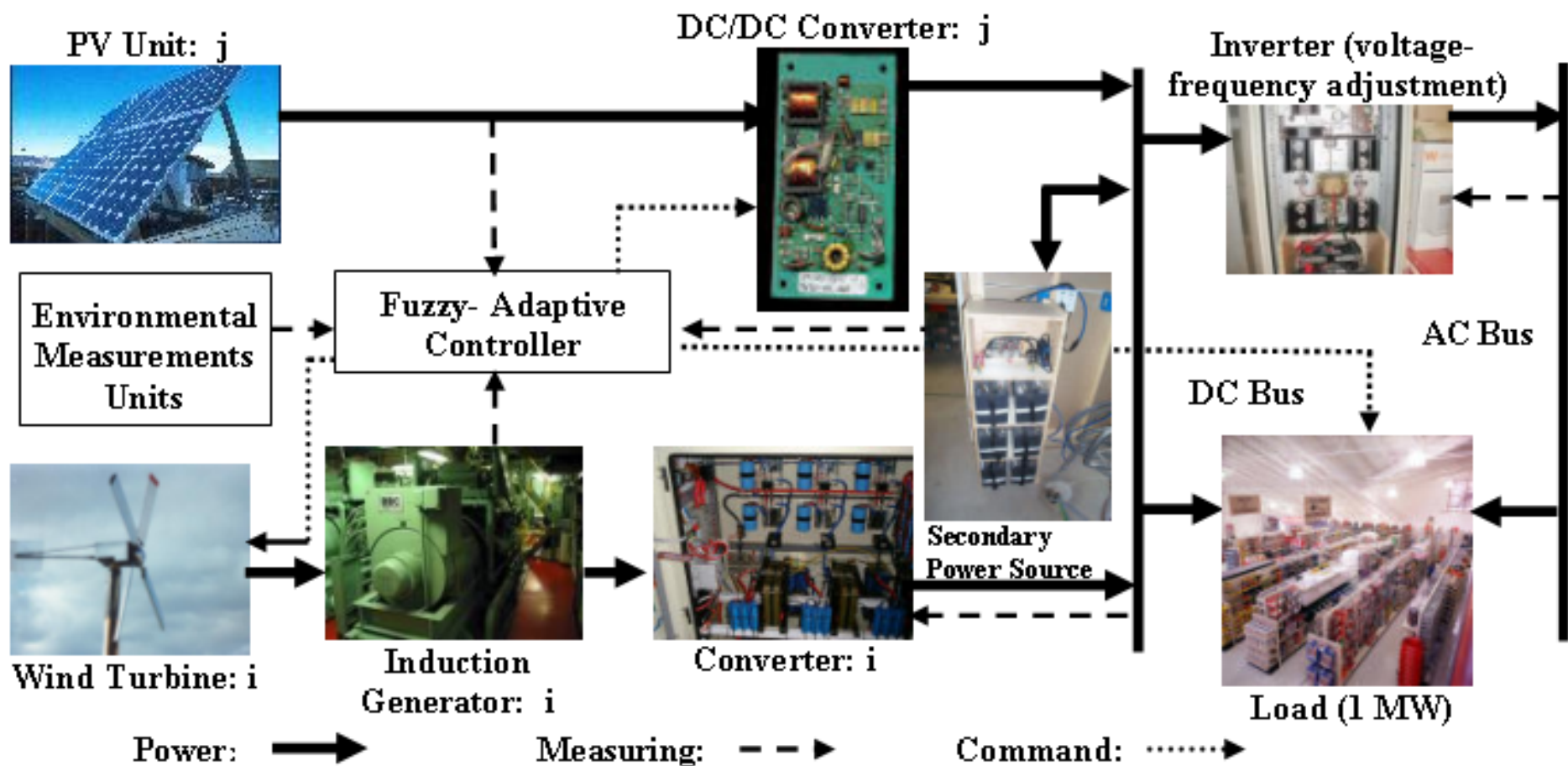
- Rapid consumption of fossil energy → Renewable sources are replacing them in many applications including smart grids.
- Main drawbacks of renewable sources are high initial cost, availability and reliability
- **This paper- hybrid PV-wind system (HPWS) with:**
  - Battery storage (to improve reliability)
  - MPPT and blade angle pitch control BAPC (to increase efficiency)
  - Optimal locations of PV and wind units
  - Optimal unit sizing

GA is used to find the best location and ratio of wind/solar contributions for a 1MVA HPWS within 256 candidate locations in USA.



# 2- Hybrid PV-Wind System

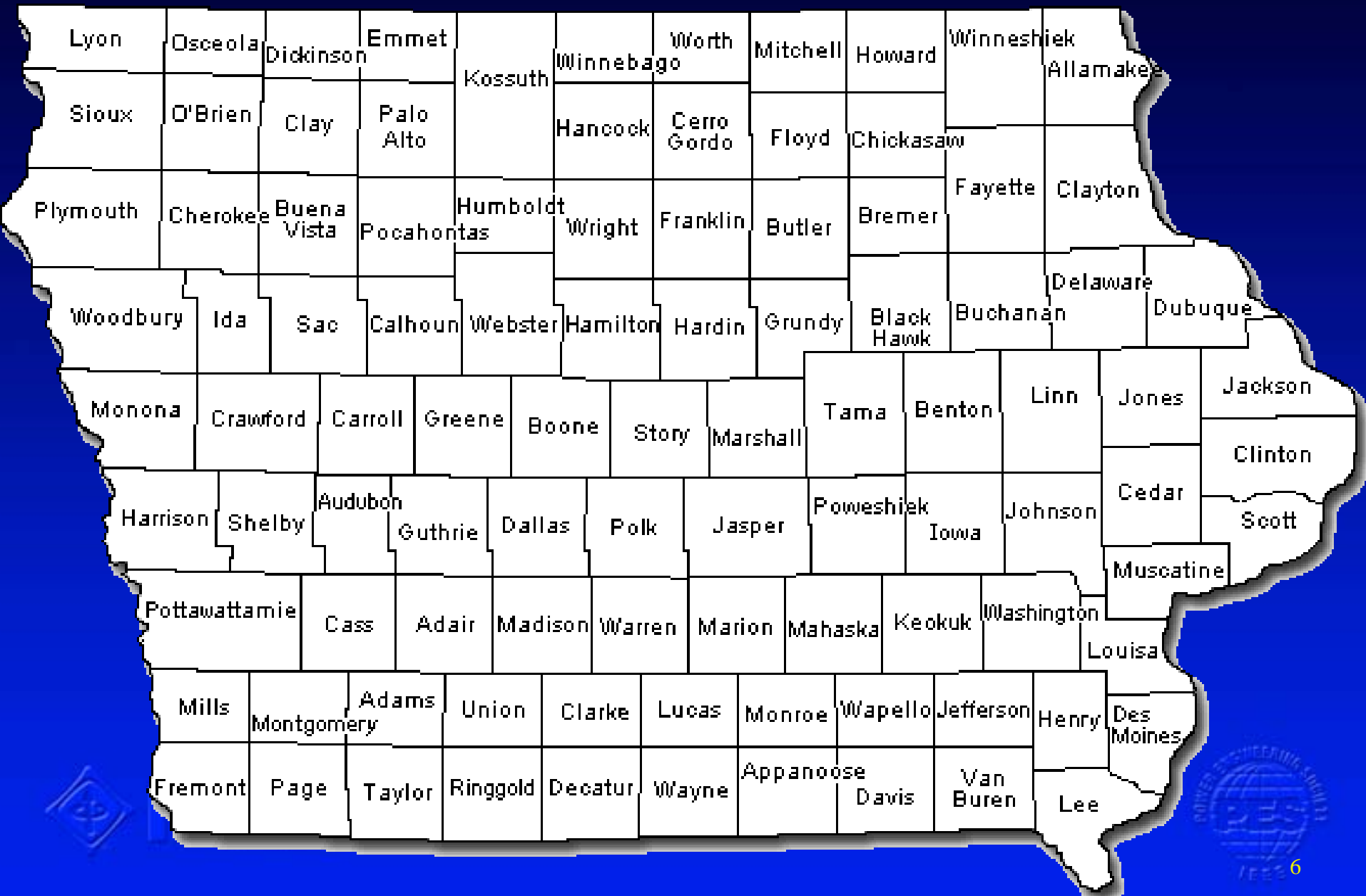
- Overall block diagram:



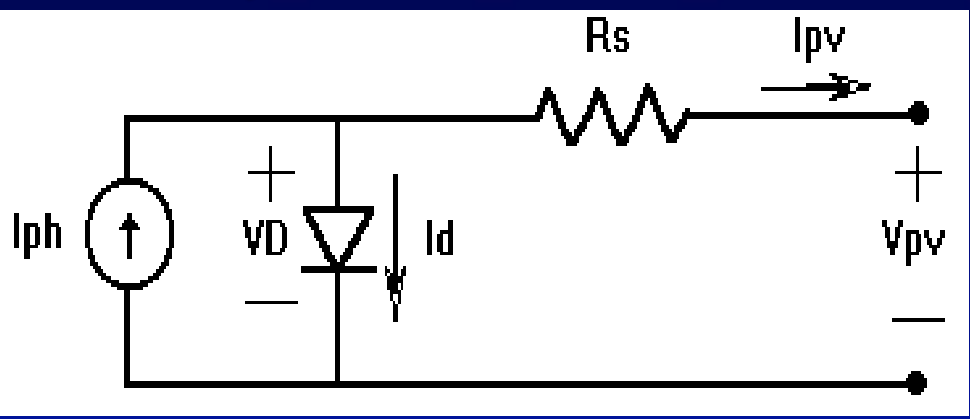
# The Hybrid PV-Wind System includes:

- Induction generator (robustness, low cost, low maintenance and greater power-weight ratio)
- VMPPT for PV (DC/DC converter)
- BAPC of wind turbines
- Three-phase bridge rectifier
- AC bus (to facilitate system application)
- Secondary power source (for excessive and emergency loading conditions)
- Fuzzy- adaptive controller and synchronization (not discussed in this paper)

# HPWS Locations Considered (Statistical Information Collected by Iowa Energy Center, [www.energy.iastate.edu](http://www.energy.iastate.edu)):

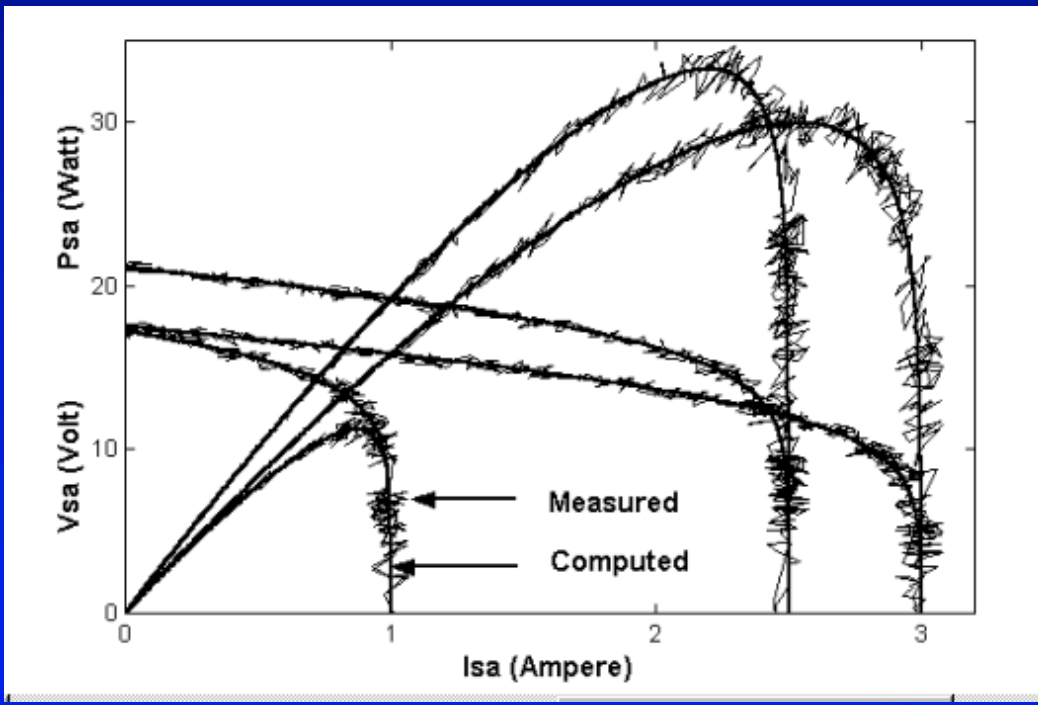


# 3- System Structure and Modeling



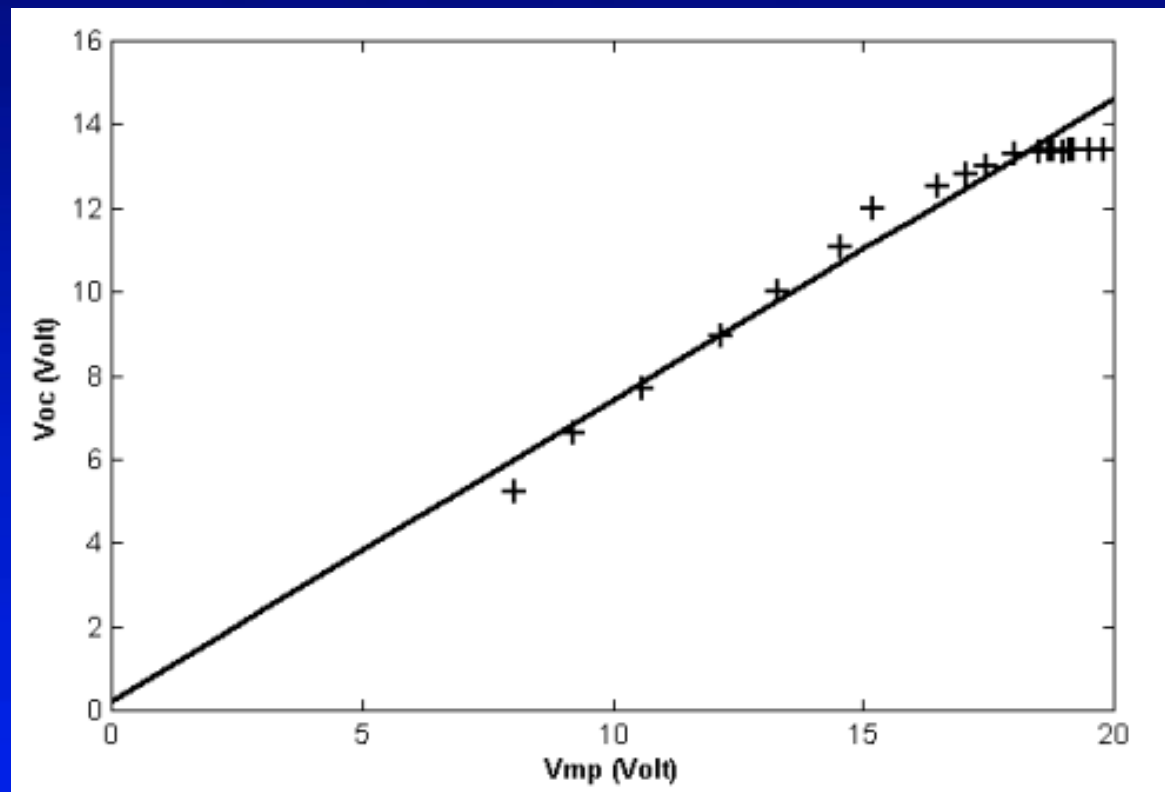
$$V_{PV} = \frac{N_s}{\lambda} \ln \left( \frac{N_p I_{ph} - i_{pv}}{N_p I_0} + 1 \right) - \frac{N_s}{N_p} R_s i_{pv}$$

Measure and computed V-I Characteristics for one OFFC panel (T=25 at varying insolation levels).

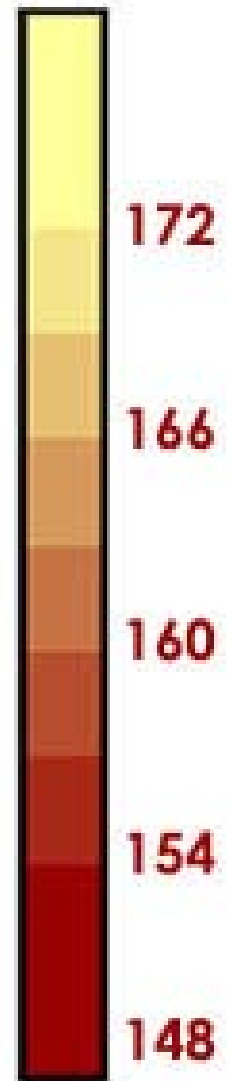
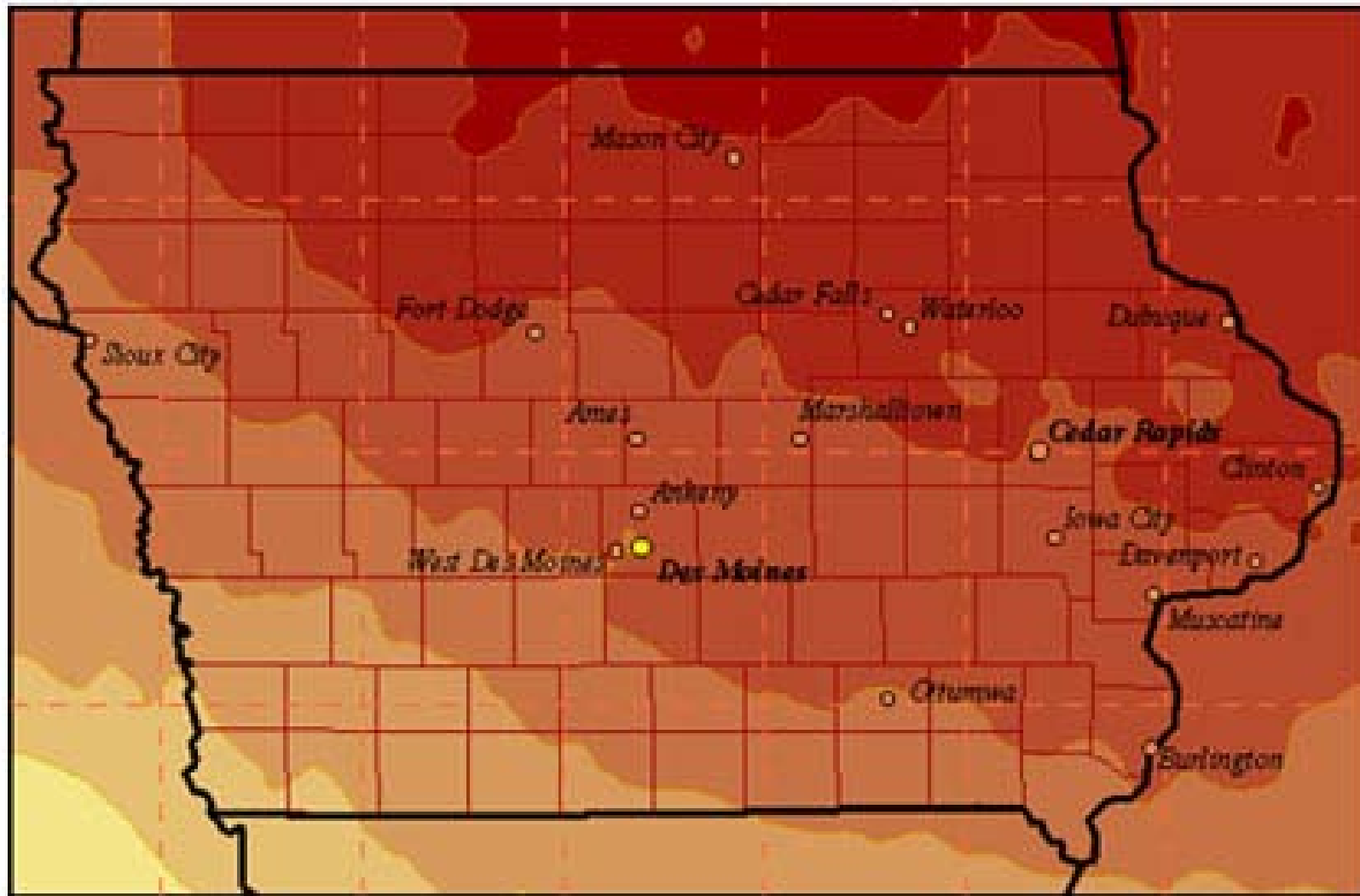


$$V_{mp} = f_{\text{nonlinear}}(V_{OC}) \cong f_{\text{linear}}(V_{OC}) = M_v \times V_{OC}$$

Dependency of "cell voltages corresponding to maximum power to "cell open-circuit voltages" for one OFFC panel (T=25 at varying insolation levels).



## Yearly Averaged Global Irradiance (Watt/sq.m)

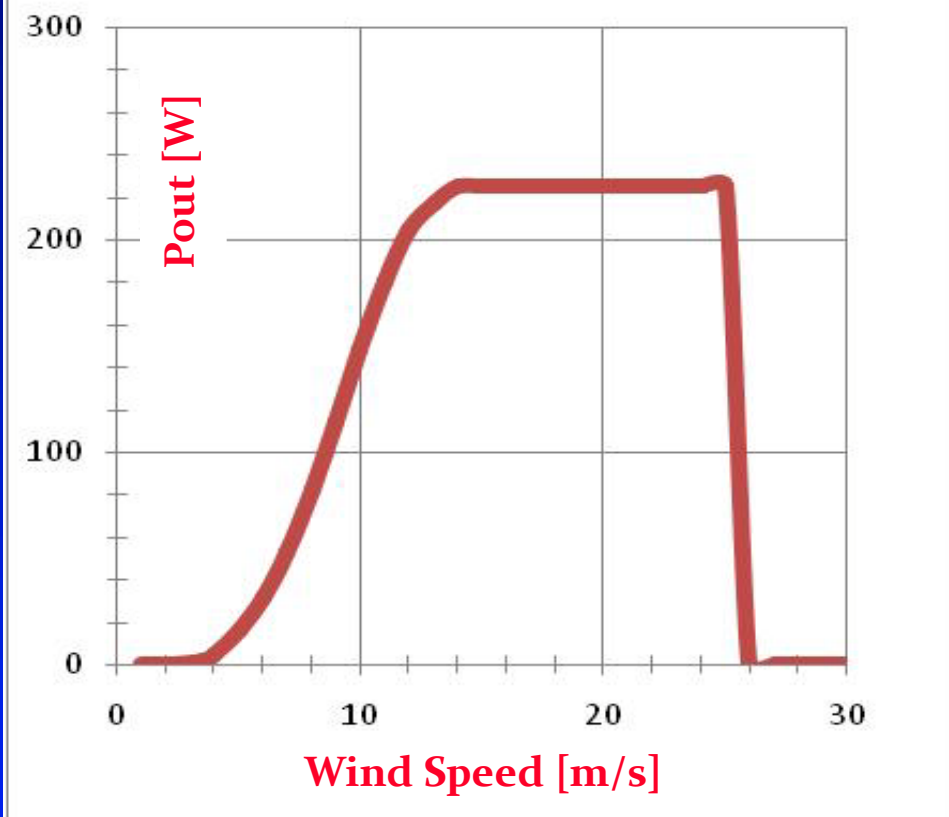


# • Wind Unit Modeling

Wind output power (Betz law):

$$P_W(v) = \begin{cases} [(v - v_c)/(v_r - v_c)]P_r & v_c \leq v \leq v_r \\ P_r & v_r \leq v \leq v_f \\ 0 & \textit{otherwise} \end{cases}$$

where  $v_r$ ,  $P_r$ ,  $v_r$  and  $v_f$  are turbines nominal speed, power, low cutoff speed and high cutoff speed, respectively.



- **Wind Unit Modeling (continue)**

**Average power produced by each wind-turbine:**

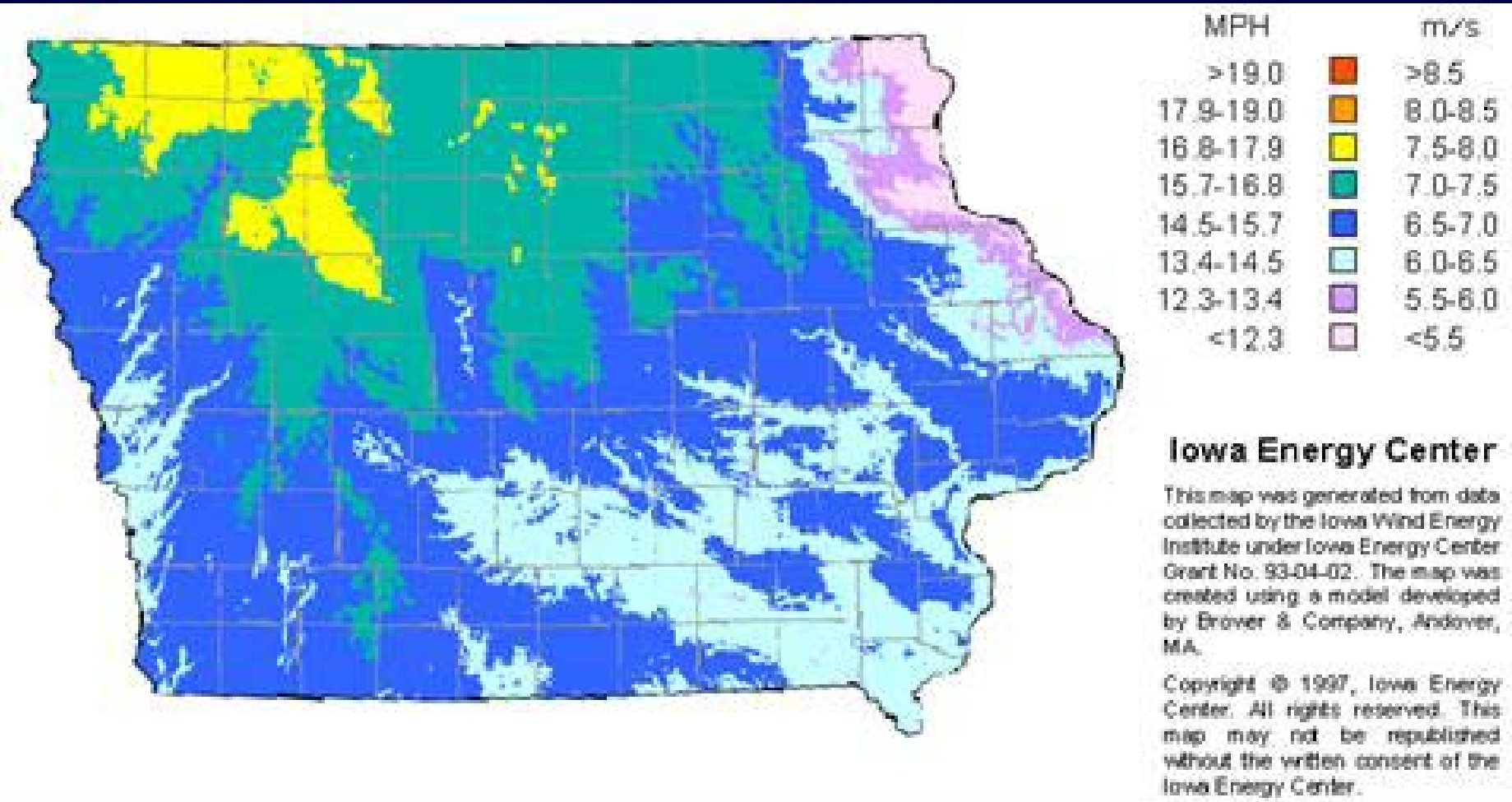
$$P_{W,avg} = \int_0^{\infty} P_w f(v) dv$$

**Where  $f(v)$  is the Weibull density function:**

$$f(v) = \frac{k}{c} \left(\frac{v}{c}\right)^{k-1} \exp\left[-\left(\frac{v}{c}\right)^k\right] (k > 0, v > 0, c > 0)$$

**where  $v$ = wind speed,  $c$ = gauge parameter =7.01m/s and  $k$ = shape parameter =1.99m/s.  $c$  and  $k$  are estimated based on the statistical computations**

- Wind Unit Modeling (continue)



- **Wind Unit Modeling (continue)**

## Technical properties of the Wind unit

Manufacture, type	Vestas225-29, lateral axes
Rated power	225 KW (in rated speed)
Rated, cut-in and cut-out speeds	14.5, 2.3, 39.3 (m/s)
Output	480 VAC/3-phase/60 HZ
Statistic function: output power (KW) – mean wind speed(m/s)	$= 21.09 v_r - 79.38$

## With:

- AC & DC loads;  $P_{\text{load-ave}} = 1 \text{ MW}$
- $P_{\text{PV-ave}} = 40 \text{ kW/unit}$
- $P_{\text{wind-ave}} = 68.46 \text{ kW/unit}$ ,

## The load may be supplied by:

$$1) n_{\text{wind-max}} = 15$$

$$2) n_{\text{PV-max}} = 25$$

3) HPWS (optimum # of PV and wind)

# 4- System Design & GA Optimization

**Cost Function:**

$$CF = \min_{l=1}^{L_{max}} (CF^l) = \min_{l=1}^{L_{max}} CF_c^l \times \frac{\min(CF_{nc}^l)}{\min(CF_c^l)}$$

$$CF_c^l = \frac{CF_{nc}^l(n_{pv}) * Lops^l(n_{pv})}{\|Lops^l(n_{pv})\|}$$

$$CF_{nc}^l = (CF_{PV}^l + CF_{Wind}^l + CF_{Sec}^l - CF_{Add}^l)$$

**Lops<sup>l</sup>** = probability of load shading at location l .

**CF<sub>nc</sub> & CF<sub>c</sub>** = total costs without/with load shading.

**CF<sub>pv</sub> & CF<sub>wind</sub>** = costs of one solar & one wind.

**CF<sub>add</sub> & CF<sub>sec</sub>** = cost of additional-available power & secondary (battery) sys.

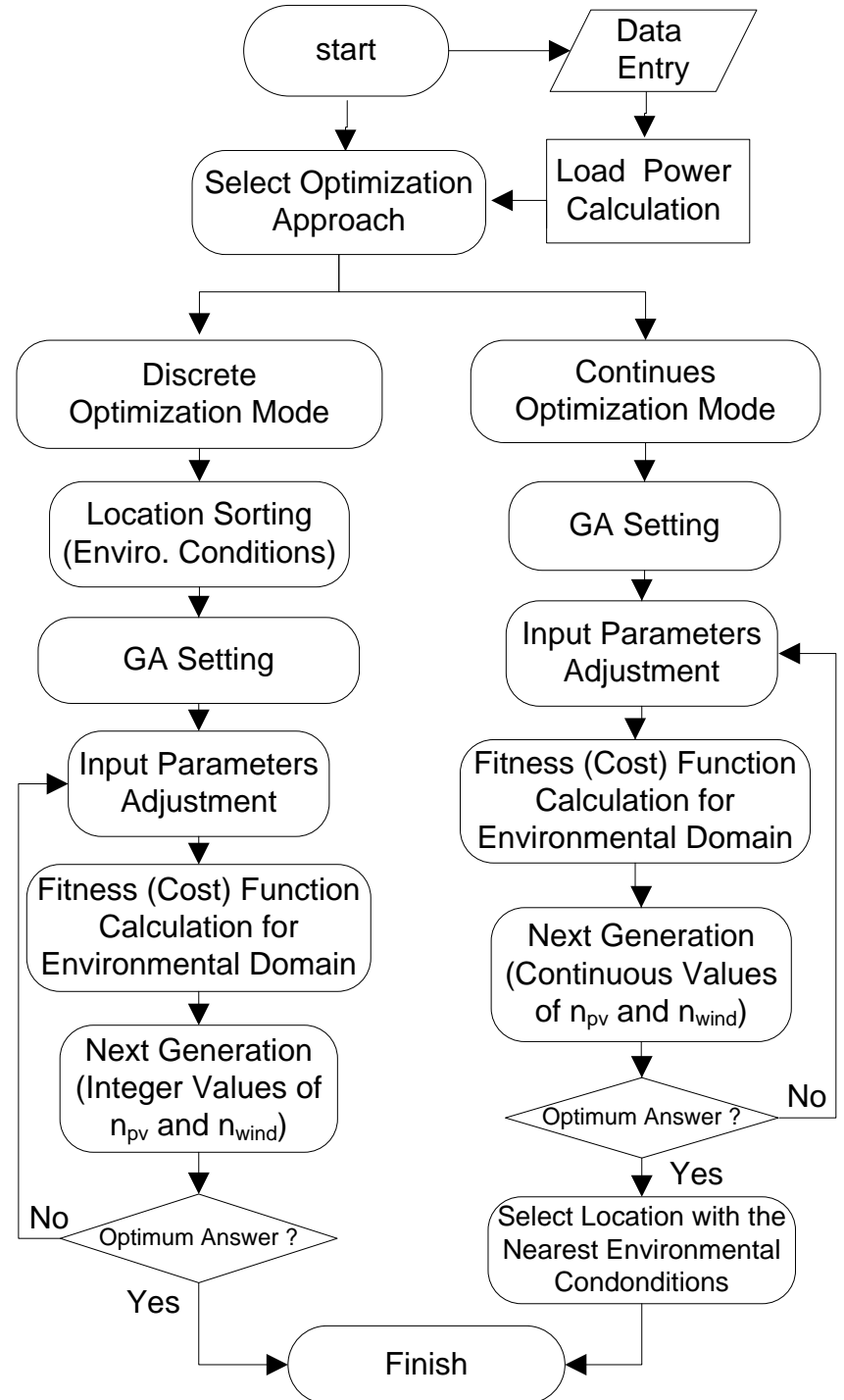
$$CF_{PV}^l = \frac{n_{PV}^l \times k_{PV} (P_{Avg-PV}^l)}{(\eta_{DC/DC}) (k_{Acc-PV}^l)}$$

$$CF_{Wind}^l = \frac{n_{Wind}^l \times k_{Wind} (P_{Avg-Wind}^l)}{(\eta_{AC/DC}) (k_{Acc-Wind}^l)}$$

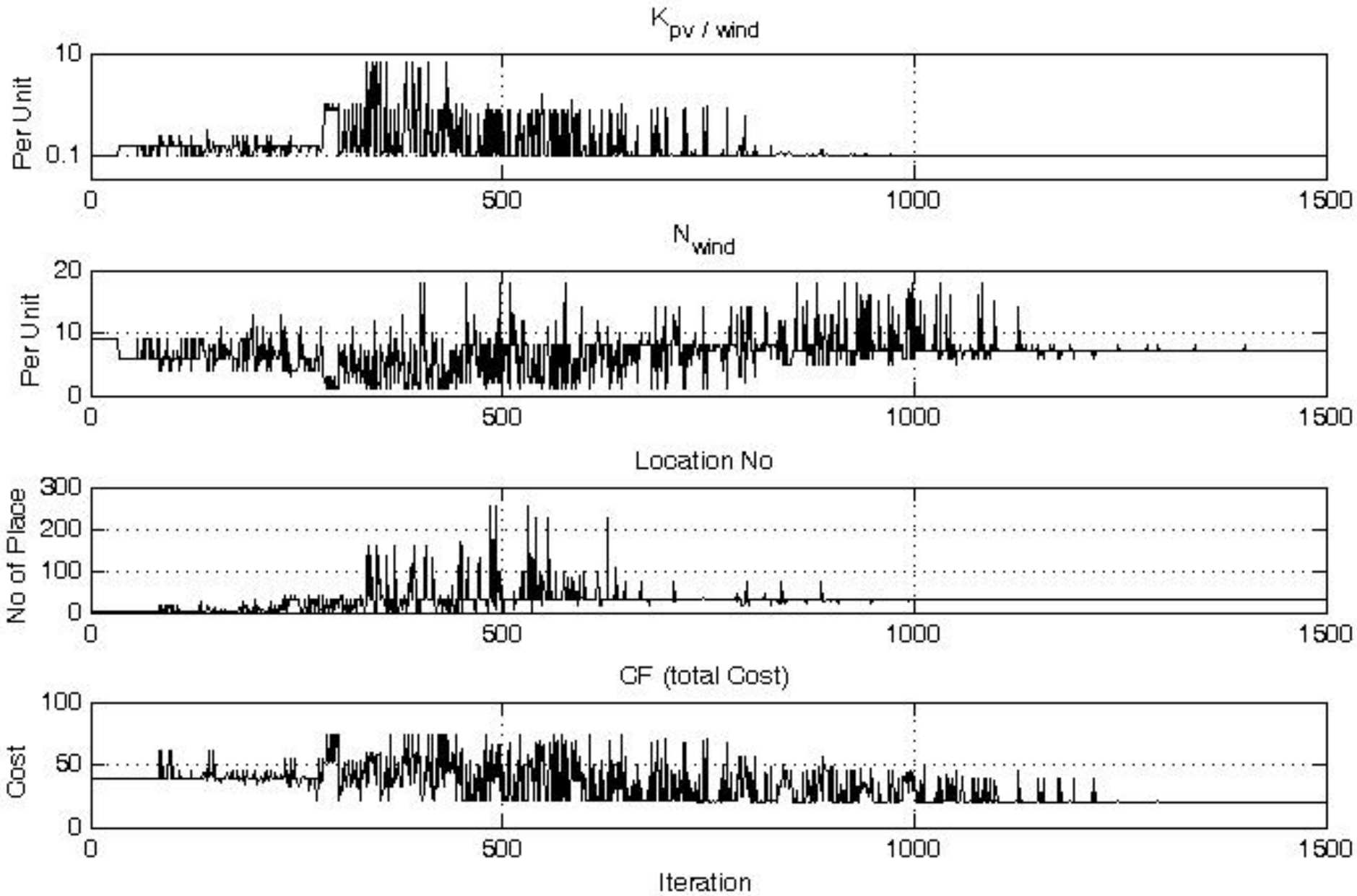
$$CF_{Sec}^l = k_{Sec} \times C_{Sec-Max}^l \times \eta_{Ch.-DisCh} / t$$

$$CF_{Add}^l = k_{Add} \times p_{Add}^l, \quad l = 1, \dots, L_{Max}$$

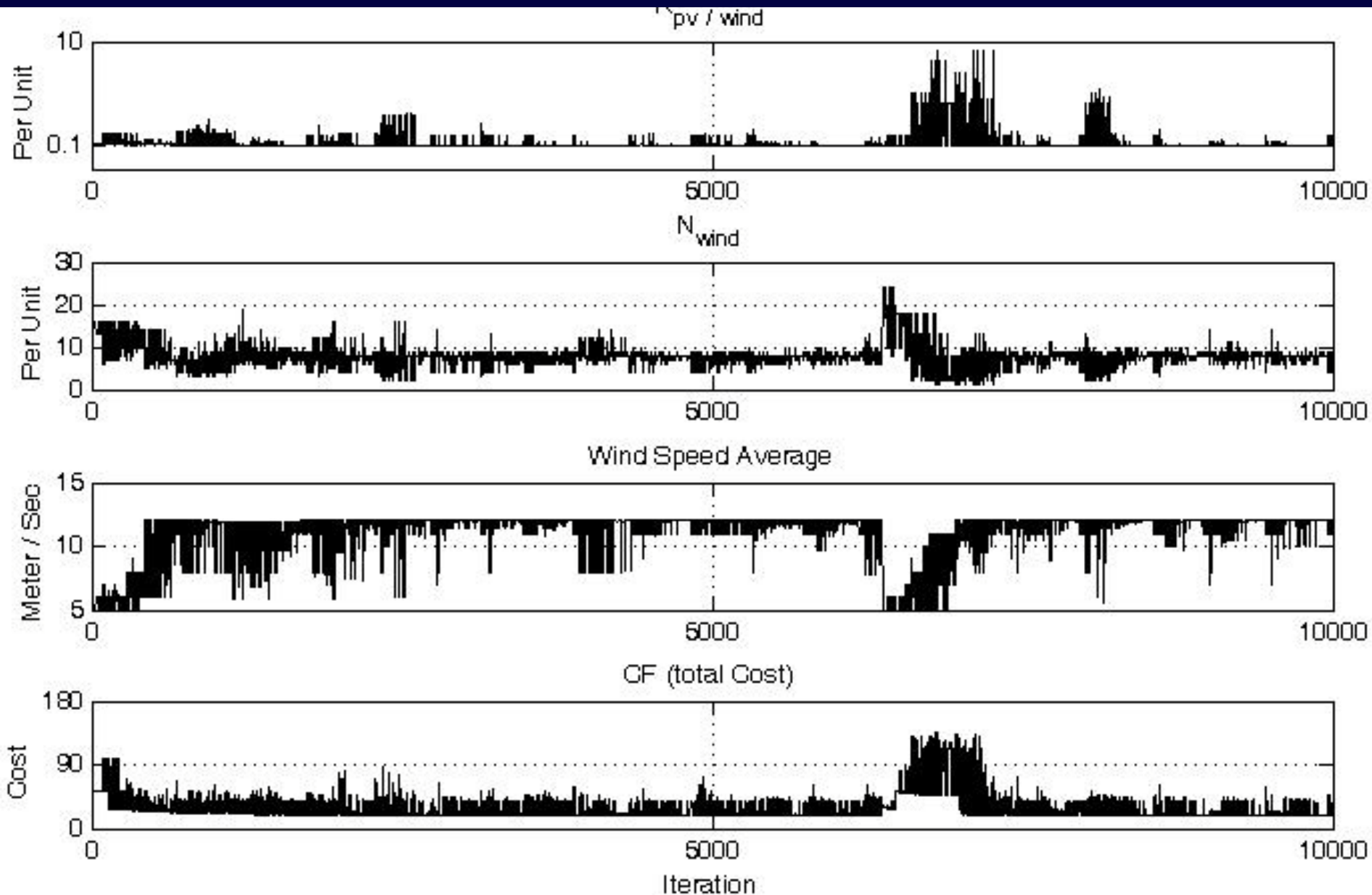
# GA Optimization



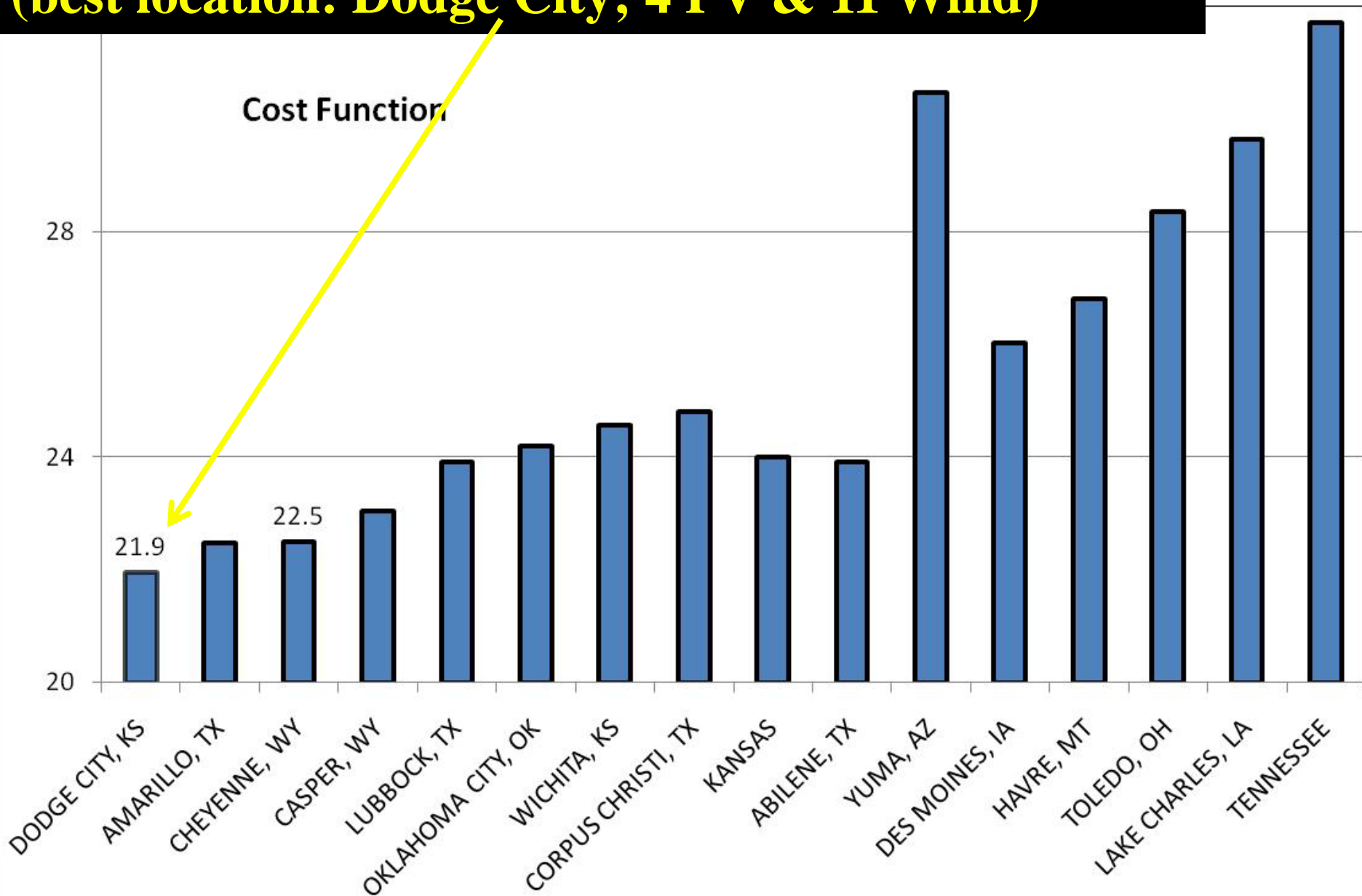
- GA Results (Discrete Mode)**



- GA Results (Continues Mode)**

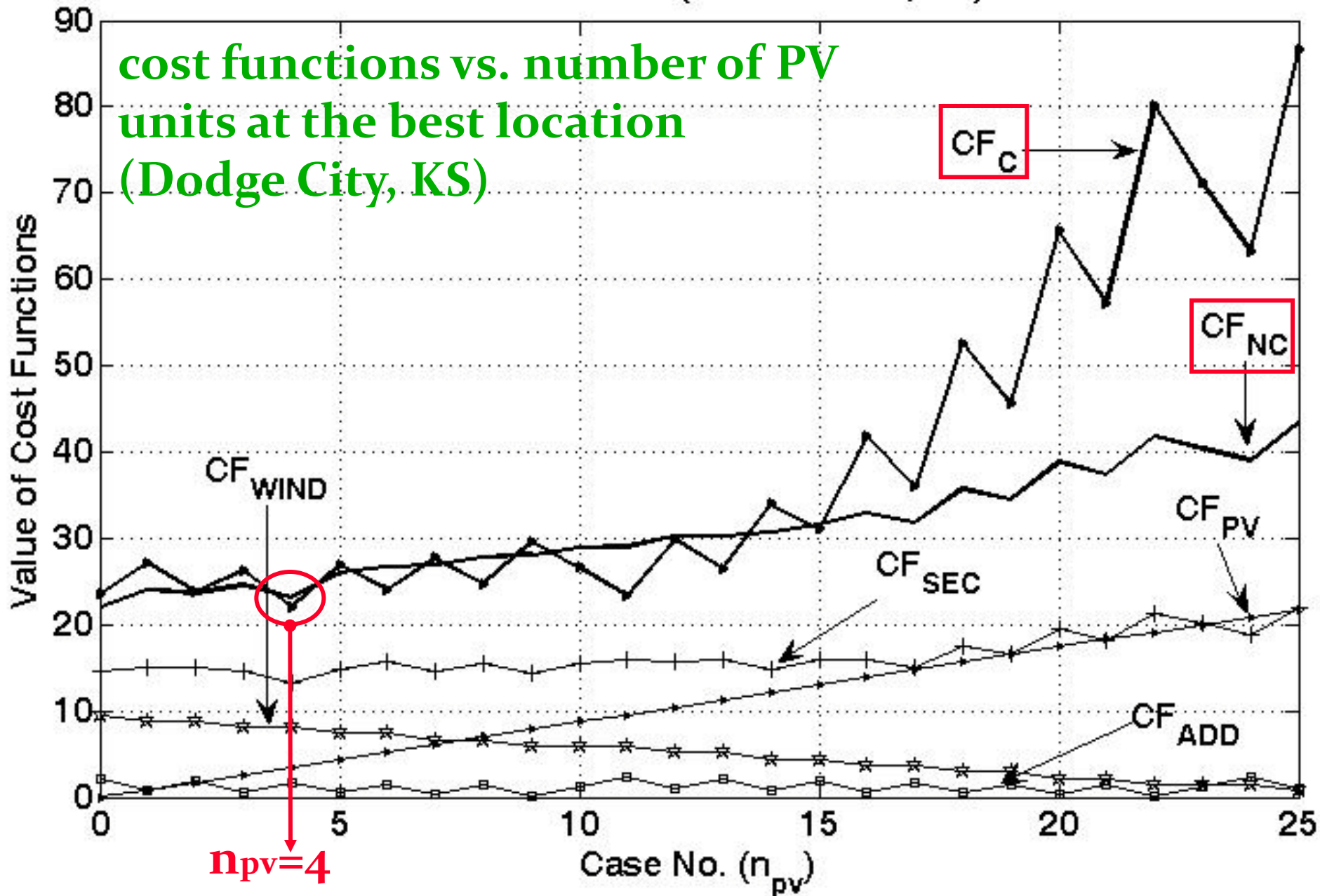


# Computed cost functions for some typical locations (best location: Dodge City; 4 PV & 11 Wind)



Location No. 91.(DODGE CITY, KS)

cost functions vs. number of PV units at the best location (Dodge City, KS)



## Recall:

**$CF_{nc}$  &  $CF_c$**  are total costs without/with load shading (at location l).

$$CF_c^l = \frac{CF_{nc}^l(n_{pv}) * Lops^l(n_{pv})}{\|Lops^l(n_{pv})\|}$$

$$CF_{nc}^l = (CF_{PV}^l + CF_{Wind}^l + CF_{Sec}^l - CF_{Add.}^l)$$

# Conclusion

**A hybrid PV-wind system is modeled that includes:**

- **MPPT of PV units and blade angle pitch control of wind turbines.**

**New cost function is defined and GA is used to find:**

- **best location of HPWS, number of PV & wind units (ratio of wind/solar power contributions).**

$$CF_{Sec}^l = k_{Sec} \times C_{Sec-Max}^l \times \eta_{Ch.-DisCh} / t,$$

$$CF_{Add}^l = k_{Add} \times P_{Add}^l, \quad l = 1, \dots, L_{Max}.$$

$$CF_{PV}^l = \frac{n_{PV}^l \times k_{PV} (P_{Avg-PV}^l)}{(\eta_{DC/DC}) (k_{Acc-PV}^l)},$$

$$CF_{Wind}^l = \frac{n_{Wind}^l \times k_{Wind}^l (P_{Avg-Wind}^l)}{(\eta_{AC/DC}) (k_{Acc-Wind}^l)},$$

**t** = operating time (hour),

**l** = location number,

**k** in numerators = statistical production cost ( $k_{wind}=0.089$ ,  $k_{PV}=0.225$ ,  $k_{Sect}=350$ ,  $k_{Add}=0.282$ ),

**k** in denominators = statistical source accessibility expense,

**n** = number of each unit,

**η** = average converters efficiency ( $\eta_{DC/DC}=0.90$ ,  $\eta_{AC/DC}=0.87$ ),

**C<sub>Batt-Max</sub>** = maximum required battery capacity under all operating conditions,

**P<sub>Add</sub>** = surplus produced power of each structure (positive energy balance) with usual electricity cost.

